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CONVERGENCE OF AUTOMORPHISMS AND SEMICONTINUITY OF AUTOMORPHISM GROUPS

Abstract

We study the compactness of the automorphism group of a domain in $\mathbb{C}^n$, and in particular the convergence properties of mappings. We supply an application to the semicontinuity of automorphism groups under perturbation of the underlying domain. Relevant examples are provided.

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